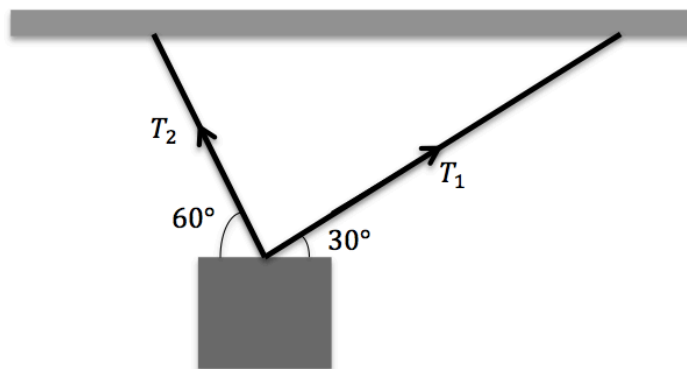


## AHMES SECONDARY SCHOOL



### FORM VI HOLIDAY PACKAGE PHYSICS

1. The number of particles  $n$  crossing a unit area perpendicular to x-axis in a unit time is given as  $n = -D \frac{(n_2 - n_1)}{(x_2 - x_1)}$  where  $n_1$  and  $n_2$  are the number of particles per unit volume for the values of  $x_1$  and  $x_2$  respectively. What are the dimensions of diffusion constant  $D$ ? **[ $L^2 T^{-1}$ ]**
2. The period of oscillation of a simple pendulum is given by  $T = 2\pi \sqrt{\frac{l}{g}}$  whereby 100 vibrations were taken to measure 200 seconds. If the least count for the time and length of a pendulum of  $1m$  is  $0.1s$  and  $1mm$  respectively. Calculate the maximum percentage error in the measurement of  $g$ . **[10.1%]**
3. A box weighing  $80N$  is supported by two wires with tension  $T_1$  and  $T_2$  as shown in the figure below. Find the tension in each wire. **[40N, 69.28N]**



4. A jet engine on a test bed takes in  $40\text{kg}$  of air per second at a velocity of  $100\text{m/s}$  and burns  $0.8\text{kg}$  of fuel per second. After compression and heating the exhaust gases are ejected at  $600\text{m/s}$  relative to the aircraft. Calculate the thrust of the engine.  
**[20480N]**
5. A spaceship is launched into a circular orbit close to the earth's surface. What additional velocity has to be imparted to the spaceship in order to overcome the gravitational pull?  
**[7926.3m/s]**
6. A particle of mass  $0.3\text{kg}$  moves with an angular velocity of  $10\text{rad/s}$  in a horizontal circle of radius  $20\text{cm}$  inside a smooth hemispherical bowl. Find the reaction of the bowl on the particle and the radius of the bowl.  
**[6.7N, 22.3cm]**
7. A wire of diameter  $0.1\text{mm}$  and resistivity  $1.69 \times 10^{-8} \Omega\text{m}$  with temperature coefficient of resistance of  $4.3 \times 10^{-3} \text{K}^{-1}$  was required to make a resistance. What length of the wire is required to make a coil with a resistance of  $0.5\Omega$ ? If on passing a current of  $2\text{A}$  the temperature of the coil rises by  $10^{\circ}\text{C}$ , what error would arise in taking the potential drop as  $1.0\text{V}$ ?  
**[23.22cm, 0.0843V]**
8. Show that the total energy of a satellite in a circular orbit equals half its potential energy.
9. A fireman standing at a horizontal distance of  $38\text{m}$  from the edge of a burning store building aimed to raise streams of water at an angle of  $60^{\circ}$  into the first floor through an open window which is at  $20\text{m}$  high from the ground level. If the water strikes on this floor  $2\text{m}$  away from the outer edge, sketch the diagram of the trajectory. At what speed will the water leave the nozzle of the fire hose?  
**[24.85m/s]**
10. A heating coil of nichrome wire with cross sectional area of  $0.1\text{mm}^2$  operate on a  $12\text{V}$  supply and has a power of  $36\text{W}$  when immersed in water at  $373\text{K}$ . Calculate the length of the wire. Temperature coefficient of resistance of nichrome is  $8 \times 10^{-5} \text{K}^{-1}$ .  
**[0.37m]**
11. A simple pendulum is suspended from the ceiling of a car taking a turn of radius  $10\text{m}$  at a speed of  $36\text{kmh}^{-1}$ . Find the angle made by the string of the pendulum with the vertical if this angle does not change during the turn.  
**[45.6^{\circ}]**
12. A hemispherical bowl of radius  $R$  is rotating about its axis of symmetry, which is kept vertical. A small block is kept in the bowl and rotates with it without slipping. If the

surface of the bowl is smooth and the angle made by the radius through the block with the vertical is  $\theta$ , show that the angular speed of the bowl is given by  $\sqrt{\frac{g \cos \theta}{R}}$

13. Prove that at a very small temperature difference,  $\Delta T = T_b - T_s$  Newton's law of cooling obeys Stefan's law whereby  $T_b$  is the temperature of the body and  $T_s$  is the temperature of the surrounding.
14. One mole of a gas expands from volume  $V_1$  to a volume  $V_2$ . If the gas obeys the Van der Waal's equation:  $(P + \frac{a}{v^2})(v - b) = RT$ , derive the formula for workdone in this process.
15. Show that the total energy of a body executing S.H.M is independent of time. Assume the initial phase is zero and the displacement equation is given by:  $y = A \sin \omega t$ .
16. If the earth were made of lead of relative density 11.3, what would be the value of acceleration due to gravity on the surface of the earth? Radius of the earth is  $6400 \text{ km}$  and  $G = 6.67 \times 10^{-11} \text{ Nm}^2 \text{ kg}^{-2}$ . **[20.2ms<sup>-2</sup>]**
17. The period  $T$  of oscillation of a body is said to be  $(1.5 \pm 0.002) \text{ s}$  while its amplitude  $A$  is  $(0.3 \pm 0.005) \text{ m}$  and the radius of gyration  $K$  is  $(0.28 \pm 0.005) \text{ m}$ . If the acceleration due to gravity  $g$  was found to be related to  $T, A$  and  $K$  by the equation:  $\frac{gA}{4\pi^2} = \frac{A^2 + K^2}{T^2}$ , find the numerical value and percentage error in  $g$ . **[(9.8393 ± 0.5293)ms<sup>-2</sup>, 5.38%]**
18. Suppose the slope of the best-fit line is 1.0 and slopes of maximum and minimum worst lines are 1.16 and 0.81 respectively. Estimate the value of slope of the graph. **[1.0 ± 0.18]**
19. A block of mass,  $m = 100 \text{ g}$  is placed on a rough inclined plane. The plane makes an angle  $\theta = 30^\circ$  with the horizontal. Determine the value of friction force that is required to keep the block at rest. **[0.49N]**
20. Due to change in main voltage the temperature of an electric bulb rises from  $3000 \text{ K}$  to  $4000 \text{ K}$ . What is the percentage change in electric power consumed? **[216%]**
21. An insect is released from rest at the top of a smooth bowling ball such that it slides over the ball. Prove that it will lose its footing with the ball at an angle of about  $48^\circ$  with the vertical.

22. A ball is projected with a velocity  $v$  at an angle  $\theta$  to the horizontal. It passes through a vertical point  $y$  and horizontal point  $x$ . If  $R$  is the horizontal range, prove that

$$\tan\theta = \frac{y}{x} \left( \frac{R}{R-x} \right)$$

23. Show that for elastic collision the kinetic energy is conserved.
24. A particle moving in S.H.M along the straight line has a velocity of  $4m/s$  when its displacement from the mean position is  $3m$  and  $3m/s$  when the displacement is  $4m$ . Find the time taken to travel  $2.5m$  from the positive extremity of its oscillation.

[1.047s]

25. A particle executes S.H.M with amplitude  $A$ . At what distance from the mean position its K.E is equal to its P.E?

[ $A/\sqrt{2}$ ]

26. A simple pendulum consists of small sphere of mass  $m$  carrying positive charge  $q$  and suspended by a thread of length  $l$ . The pendulum is placed in a uniform electric field of strength  $E$  directed vertically upwards. If the electrostatic force acting on the sphere is less than the gravitational force, show that the period of oscillation is given

$$\text{by: } T = 2\pi \sqrt{\frac{l}{(g-qE/m)}}$$

27. Imagine a tunnel is dug along a diameter of the earth. Show that a body dropped from one end of the tunnel executes S.H.M. What is the time period of this motion? Assuming the earth to be a sphere of uniform density  $\rho = 5520kgm^{-3}$  and  $G = 6.67 \times 10^{-11} Nm^2kg^{-2}$ .

[5059.45s]

28. In the first second of its flight a rocket ejects  $\frac{1}{60}$  of its mass with a relative velocity of  $2400ms^{-1}$ . Find its acceleration. What is the final velocity if the ratio of initial to final mass of the rocket is 4 at a time of 60 seconds?

[ $30ms^{-2}$ ,  $2727ms^{-1}$ ]

29. A model airplane  $X$  has a mass of  $0.5kg$  and has a control wire  $OX$  of length  $10m$  attached to it when it flies in horizontal circle with wings horizontal. The wire  $OX$  is inclined  $60^\circ$  to the horizontal and fixed to a point  $O$  and  $X$  takes  $2s$  once round its circular path. Calculate the tension in the control wire and the upward force on  $X$  due to the air.

[49.35N, 47.64N]

30. Prove that minimum height at which the body has to be released on a smooth loop-looping apparatus in order for it to successfully complete the circular loop is given by  $\frac{5}{2}R$ , where  $R$  is radius of the loop.
31. An artificial satellite of mass  $M$  travels around the earth just above the surface (very close to earth's surface). Find the length of the simple pendulum that will have the same period as that of the satellite. (Give your answer in terms of the diameter of the earth). **[ $l = D/2$ ]**
32. Use work-energy theorem in rotational motion to show that torque for a rotating rigid body is given by:  $\tau = I\alpha$
33. An aluminium foil of relative emittance 0.2 is placed between two concentric spheres at temperatures 300K and 200K respectively. Calculate the temperature of the foil after the steady state is reached. Also calculate the rate of energy transfer between one of the spheres and the foil. Stefan's constant,  $\sigma = 5.67 \times 10^{-8} \text{Wm}^{-2}\text{K}^{-4}$ .  
**[263.9K, 36.85Wm<sup>-2</sup>]**
34. What amount of heat is to be transfer to nitrogen in an isobaric heating so that the gas may perform 2J of work? Atomicity,  $\gamma = 1.4$  **[7J]**
35. Show that the slope of an adiabatic curve is always greater than that of an isothermal curve.
36. Show that the drift velocity acquired by electrons in a conductor is given by:  $v_d = \frac{I}{neA}$  where all symbols carry their usual meaning.
37. Briefly explain three techniques applicable for improving plant environment for better plant growth.
38. The reading of a pressure meter attached with closed water pipe is  $4 \times 10^5 \text{N/m}^2$ . On opening the valve of the pipe, the reading of pressure meter is reduced to  $3.2 \times 10^5 \text{N/m}^2$ . Calculate the speed of water flowing in the pipe. **[12.65ms<sup>-1</sup>]**
39. A hydrometer has a cylindrical glass stem of diameter 0.50cm. It floats in water of density  $1000 \text{kg/m}^3$  and surface tension  $7.2 \times 10^{-2} \text{N/m}$ . A drop of liquid detergent added to the water reduces the surface tension to  $5.0 \times 10^{-2} \text{N/m}$ . What will be the change in length of the exposed portion of the glass stem? Assume that the relevant angle of contact is always zero. **[1.8mm]**

40. A heavy rigid bar is supported horizontally from a fixed support by two vertical wires A and B, of the same initial length and which experience the same extension. If the ratio of diameter of A to that of B is 2 and the ratio of Young's modulus of A to that of B is 2. Calculate the ratio of the tension in A to that in B. If the distance between the wires is  $d$ , calculate the distance of wire A from the center of gravity of the bar.

[8,  $d/9$ ]

41. Parallel metal plates 3mm apart carry equal and opposite charge densities of  $\pm 2\mu C/m^2$ . A proton is released from rest at the positive plate. What is the speed of proton just as it strikes the negative plate? Mass of proton,  $m_p = 1.67 \times 10^{-27} kg$  and  $e = 1.6 \times 10^{-19} C$ .

42. The equation  $y = a \sin(\omega t - kx)$  represents a plane wave travelling in a medium along  $x$  direction,  $y$  being the displacement at the point  $x$  at time  $t$ . Deduce whether the wave is travelling in the positive or in the negative  $x$  direction. If  $a = 1.0 \times 10^{-7} m$ ,  $\omega = 6.6 \times 10^3 rad s^{-1}$  and  $k = 20 m^{-1}$ , calculate the speed of the wave, the maximum speed of the particle of the medium due to the wave and the phase difference between two positions of the same particle in an interval of 0.25s.

[**Positive  $x$  – direction,  $330 ms^{-1}$ ,  $6.6 \times 10^{-4} ms^{-1}$ ,  $1650 rad$** ]

43. Four charges of +4, -3, +2 and +3 coulomb are placed at the corners of a square of each side 1m. Find the electric field at the centre of the square. Permittivity of free space,  $\epsilon_0 = 8.85 \times 10^{-12} F m^{-1}$ .

[ **$1.138 \times 10^{11} NC^{-1}$** ]

44. A police car's siren emits a sinusoidal wave with frequency 300Hz. The speed of sound is 340m/s and the air is still. Find the wavelength of the waves in front of and behind the siren if the car is moving at 30m/s.

[**1.03m, 1.23m**]

45. The face of lens has radius of curvature of 50cm. It is placed in contact with flat plate and Newton's rings are observed normally with reflected light of wavelength  $5 \times 10^{-6} cm$ . Calculate the radii of the fifth and tenth bright rings.

[**0.034cm, 0.049cm**]

46. A radioactive source in the form of a metallic sphere of radius 1.0cm emits  $\beta$  particles at the rate of  $5 \times 10^{10}$  particles per second. If the source is electrically insulated, how long will it take for its electric potential to be raised by 2V? Assuming

that 40% of the emitted  $\beta$  particles escape the source. Given  $\epsilon_0 = 8.85 \times 10^{-12} \text{ Fm}^{-1}$ ,  
 $e = 1.6 \times 10^{-19} \text{ C}$  **[0.46ms]**

47. A small speaker emitting a note of frequency  $250 \text{ Hz}$  is placed over the open upper end of a vertical tube that is full of water. When the water is gradually run out of the tube the air column resonates. If the initial and final positions of water surface below the top are  $0.31 \text{ m}$  and  $0.998 \text{ m}$  respectively, calculate the speed of sound in air and the end correction of the tube. **[334ms<sup>-1</sup>, 0.034m]**

48. A lagged copper rod is uniformly heated by a passage of an electric current. Show by considering a small section  $dx$  that the temperature  $\theta$  varies with distance  $x$  along a rod in a way that,  $H = -k \left( \frac{d^2\theta}{dx^2} \right)$  where  $k$  is the thermal conductivity and  $H$  is the rate of heat generation per unit volume.

49. A cup of tea kept in a room with a temperature of  $22^\circ \text{ C}$  cools from  $66^\circ \text{ C}$  to  $63^\circ \text{ C}$  in  $1 \text{ minute}$ . How long will the same cup of tea take to cool from the temperature of  $43^\circ \text{ C}$  to  $40^\circ \text{ C}$  under the same condition? **[2.2min]**

50. A capacitor  $C_1$  is charged to a potential difference  $V_1$ . The charging battery is removed and the capacitor is then connected to uncharged capacitor  $C_2$ . What is the final potential difference  $V$  across the combination? Find the stored energy before and after the switch is thrown and the energy loss.

$$\left[ V = \frac{C_1 V_1}{(C_1 + C_2)}, E_i = \frac{C_1 V_1^2}{2}, E_f = \frac{C_1 V_1^2}{2(C_1 + C_2)} \right]$$

51. The spherical shell of Van de Graff generator is to be charged to a potential of  $10^6 \text{ V}$ . Calculate the minimum radius of the shell if the dielectric strength of air is  $3 \times 10^6 \text{ Vm}^{-1}$ . **[0.33m]**

52. In a Van de Graff generator, the shell electrode is at  $25 \times 10^5 \text{ V}$ . The dielectric strength of the gas surrounding the electrode is  $5 \times 10^7 \text{ Vm}^{-1}$ . Calculate the minimum radius of the spherical shell. **[5cm]**

53. Sketch a graph to show how a charge  $Q$  varies with time  $t$  during discharging process of a capacitor. What is the significance of the gradient at any point along the graph?

**[Gradient represents discharge current]**

54. A cell of e.m.f  $E$  and internal resistance  $r$  is used to drive current  $I$  through a load resistance  $R$ . Show that for maximum electric power to be transferred to the load, a load resistance  $R$  must be equal to the internal resistance  $r$  of the cell.
55. An open pipe of length  $15\text{cm}$  and a pipe of length  $11.5\text{cm}$  closed at one end are both surrounding their first overtones. If their notes are of the same frequency, what will be the end correction of the two pipes? State assumption made in arriving at your answer. **[0.5cm, Assumption: Pipes are of the same radius]**
56. A particle rests on a horizontal platform that is moving vertically in simple harmonic motion with amplitude of  $50\text{mm}$ . If above a certain frequency the particle ceases to remain in contact with the platform throughout the motion. Determine the lowest frequency at which this situation will occur. At what position will the particle cease to remain in contact with the platform? **[2.23Hz, At highest position]**
57. A capacitor of capacitance  $300\mu\text{F}$  is connected in parallel with another capacitor of unknown capacitance  $C$ . The combination discharges through a resistor of  $360\Omega$  with a time constant of 180 seconds. Calculate the value of unknown capacitance  $C$ . What will be the time constant if the capacitors above are connected in series? **[200 $\mu\text{F}$ , 43.2s]**
58. Show that the unit of  $CR$  (time constant) is seconds and prove that for a discharging capacitor it is the time taken for the charge to fall by 37%.
59. A capacitor of  $12\mu\text{F}$  is connected in series with a resistor of  $0.7\text{M}\Omega$  across a  $250\text{V}$  dc supply. Calculate the initial charging current and potential difference across the capacitor after 4.2 seconds. **[0.36mA, 98.4V]**
60. Prove that if two spherical shells of a spherical capacitor have their radii approximately equal, the device approximates a parallel plate capacitor.
61. Ice is forming on the surface of a pond. When it is  $4.6\text{cm}$  thick the temperature of the ice in contact with the air is  $260\text{K}$  while the surface in contact with the water is at temperature  $273\text{K}$ . Find the rate at which the thickness of the ice is forming. Given  $\rho_{ice} = 920\text{kgm}^{-3}$ ,  $k_{ice} = 1.6\text{Wm}^{-1}\text{K}^{-1}$  and  $L_{ice} = 334,000\text{Jkg}^{-1}$  **[1.47 $\times 10^{-6}\text{ms}^{-1}$ ]**
62. Two spherical soap bubbles of radii  $30\text{mm}$  and  $10\text{mm}$  coalesce so that they have a common surface. If they are made from the same solution and the radii of the bubbles



remain the same after they join together, derive the formula for radius of curvature of their common interface and find its value.

$$[r = \frac{r_1 r_2}{r_1 - r_2}, \mathbf{15mm}]$$

63. An electron beam passes through parallel plate capacitor with a velocity of  $10^7 \text{ms}^{-1}$ . The length of each plate is  $10\text{cm}$  while the distance between the plates is  $5\text{cm}$ . Calculate the deflection angle of the beam if the electric intensity between the plates is  $20\text{Vcm}^{-1}$ . Given  $e = 1.6 \times 10^{-19}\text{C}$  and  $m_p = 1.67 \times 10^{-27}\text{kg}$   $[\theta = \mathbf{19.37^\circ}]$
64. A stationary wave is given by  $y = 5\sin\frac{\pi x}{3}\cos 40\pi t$ , where  $x$  and  $y$  are in  $\text{cm}$  and  $t$  is in seconds. What are the equations of the component waves whose superposition gives rise to the above wave?  $[y_1 = \frac{5}{2}\sin\left(\frac{\pi}{3}x - 40\pi t\right), y_2 = \frac{5}{2}\sin\left(\frac{\pi}{3}x + 40\pi t\right)]$
65. The e.m.f (in microvolts) in a lead-iron thermopile, one junction of which is at  $0^\circ\text{C}$  is given by  $V = 1784t - 2.4t^2$ , where  $t$  is the temperature of the hot junction. Calculate the neutral temperature.  $[\mathbf{3717^\circ\text{C}}]$
66. A uniform spring has a certain mass suspended from it and its period for vertical oscillation is  $T_1$ . The spring is now cut into two equal halves and the same mass is suspended from one of the halves. The period of vertical oscillation is now  $T_2$ . Calculate  $T_2/T_1$ ?  $[\sqrt{\mathbf{1/2}}]$
67. Two similar balls of mass  $m$  are hung from silk threads of length  $a$  and carry similar charge  $q$ . Assume  $\theta$  is small enough that  $\tan\theta = \sin\theta$ . To this approximation, show that:  $x = \left(\frac{q^2 a}{2\pi\epsilon_0 m g}\right)^{\frac{1}{3}}$  where  $x$  is the distance of separation.
68. Show that the radial heat flow across the coaxial cylinder is given by  $H = \frac{2\pi KL(T_2 - T_1)}{\ln\left(\frac{r_2}{r_1}\right)}$   
where  $K$  is the thermal conductivity,  $L$  is the length of the cylinder,  $r_1$  and  $r_2$  are the radii of inner and outer parts of the cylinder respectively.
69. There are two angles of projection for which the horizontal range is the same. Show that the sum of the maximum heights for these two angles is independent of the angle of projection.
70. A large open tank has two holes in the wall. One is a square of side  $l$  at a depth  $y$  from the top and the other is a circular hole of radius  $r$  at a depth  $4y$  from the top.

When the tank is completely filled with water the quantities of water flowing out per second from both holes are the same. Find the value of the radius.  $[l/\sqrt{2\pi}]$

71. If the energy required to blow a soap bubble of radius  $r$  is  $E$ , show that the extra energy needed to double the radius of the bubble is given by  $\Delta E = 24\pi\gamma r^2$  where  $\gamma$  is the surface tension.

72. A horizontal tube A of length  $50\text{cm}$  and radius of  $0.1\text{mm}$  is joined to another horizontal tube B of length of  $40\text{cm}$  and radius  $0.2\text{mm}$ . If a liquid passing through the tubes enters A at a pressure of  $85\text{cm}$  of mercury and leaves B at a pressure of  $76\text{cm}$  of mercury. What the pressure in  $\text{Nm}^{-2}$  at the junction of tubes?

$$[1.019 \times 10^5 \text{Nm}^{-2}]$$

73. Ultrasound of frequency  $4.0\text{MHz}$  is incident at an angle of  $30^\circ$  to a blood vessel of diameter  $1.6\text{mm}$ . If a doppler shift of  $3.2\text{kHz}$  is observed. Calculate the blood flow velocity. Assume that the speed of ultra sound is  $1.5\text{km/s}$ .  $[0.69\text{ms}^{-1}]$

74. An X-ray unit operating at  $100\text{kV}$  produces a current of  $20\text{mA}$ . Use this information to calculate:

(i) The number of electrons striking the target per second  $[1.27 \times 10^{17} \text{electrons/s}]$

(ii) The speed of electrons incident on the target.  $[1.87 \times 10^8 \text{m/s}]$

(iii) The lowest wavelength of the continuous X-ray spectra.  $[1.24 \times 10^{-11} \text{m}]$

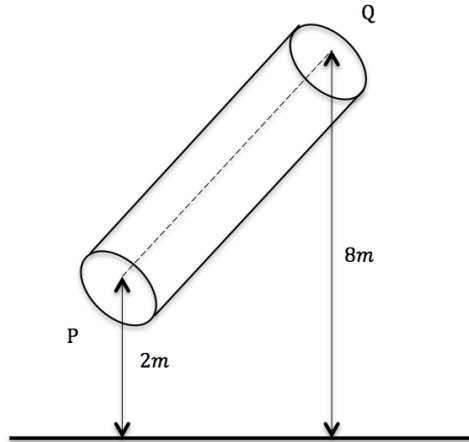
75. The half-life of *Strontium* – 90 is  $28.8\text{years}$ . Find

(i) Its decay constant in seconds.  $[7.63 \times 10^{-10} \text{s}^{-1}]$

(ii) The initial activity of  $4\text{g}$  of strontium.  $[2.04 \times 10^{13} \text{Bq}]$

(iii) How much activity will be remaining after 4 half lives.  $[1.275 \times 10^{12} \text{Bq}]$

76. A non-viscous fluid of constant density  $1000\text{kg/m}^3$  flows in a streamline motion along a tube of variable cross-section. The tube is kept inclined in the vertical plane as shown in figure below. The area of cross-section of the tube at two points P and Q at heights  $2\text{m}$  and  $5\text{m}$  are respectively  $4 \times 10^{-3}\text{m}^2$  and  $8 \times 10^{-3}\text{m}^2$ . The velocity of the fluid at point P is  $1\text{m/s}$ . Find the work done per unit volume by gravity and pressure forces as the liquid flows from point P to Q.  $[29025\text{Jm}^{-3}]$



77. A vertical capillary tube  $10\text{cm}$  long tapers uniformly from an internal diameter of  $1\text{mm}$  at the lower end to  $0.5\text{mm}$  at the upper end. The lower end is just touching the surface of a pool of liquid of surface tension  $6 \times 10^{-2}\text{N/m}$ , density  $1200\text{kgm}^{-3}$  and zero angle of contact with the tube. Calculate the capillary rise, justifying your method. **[2.3cm]**
78. A long straight conductor P carrying a current of  $2\text{A}$  is placed parallel to a short conductor Q of length  $0.05\text{m}$  carrying a current of  $3\text{A}$ . The two conductors are  $0.1\text{m}$  apart. Calculate the flux density due to P at Q and the approximate force on Q. **[ $4 \times 10^{-6}\text{T}$ ,  $6 \times 10^{-7}\text{N}$ ]**
79. An electron moving along the  $+x$  axis at a speed  $v = 5.5 \times 10^6\text{m/s}$  enters a uniform magnetic field that makes an angle of  $72^\circ$  with the  $+x$  axis. If the magnitude of magnetic field is  $0.32\text{T}$ , calculate:
- (i) The pitch **[0.19mm]**
  - (ii) The radius of trajectory **[0.093mm]**
  - (iii) The time required for one trip around the helix **[ $1.12 \times 10^{-10}\text{s}$ ]**
80. Find the current through a loop need to create a maximum torque of  $11.8\text{Nm}$ . The loop has 100 square turns each of length  $22\text{cm}$  and placed in a uniform magnetic field of magnitude  $0.96\text{T}$ . **[40.63A]**
81. A toroid of 1200 turns with an air core has a radius of  $15\text{cm}$  and cross section area of  $12\text{cm}^2$ . What is the self inductance of the coil? **[ $2.3 \times 10^{-3}\text{H}$ ]**
82. (i) What are the sources of heat energy within the interior of the earth?

(ii) What are the factors that influence the flow of heat from the interior of the earth?

83. A transmitting antenna at the top of the tower has a height of  $32m$  and that of receiving antenna is  $50m$ . What is the maximum distance between them for the satisfactory communication in line of sight? **[45536.8m]**

84. Consider a common base transistor, prove that:

$$Power\ gain = Current\ gain \times Voltage\ gain$$

85. When light of frequency  $5.4 \times 10^{14} Hz$  is shone on metal surface the maximum energy of the electrons emitted is  $1.2 \times 10^{-19} J$ . If the same surface is illuminated with light of frequency  $6.6 \times 10^{14} Hz$ , the maximum energy of the electrons emitted is  $2.0 \times 10^{-19} J$ . Calculate the value of Plank's constant and work function in  $eV$ . **[6.67 × 10<sup>-34</sup> Js, 1.5eV]**

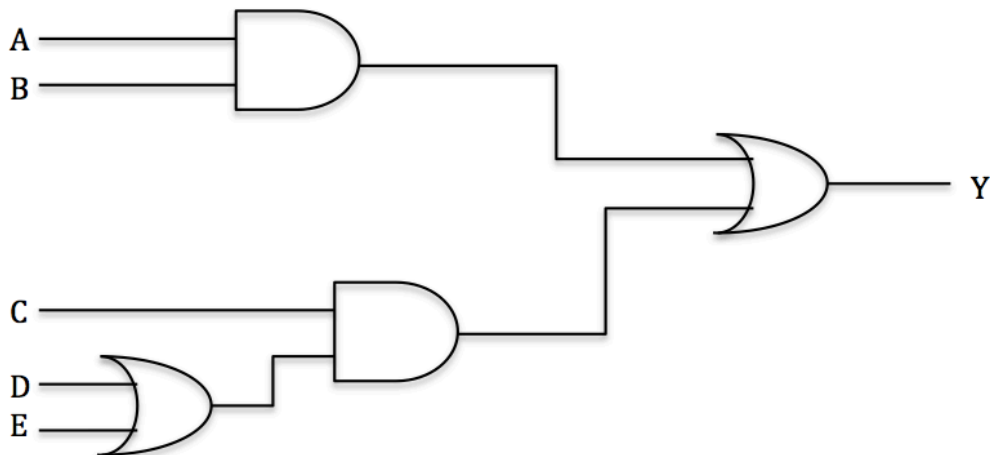
86. Consider the alpha decay equation:  ${}^{226}_{88}Ra \rightarrow {}^{222}_{86}Rn + {}^4_2He + Q$   
Given the masses are  $226.0254u$  for  ${}^{226}_{88}Ra$ ,  $222.0175u$  for  ${}^{222}_{86}Rn$  and  $4.0026u$  for  ${}^4_2He$ .

(i) Calculate the  $Q$  value for this process. **[4.94MeV]**

(ii) Calculate the kinetic energy of the alpha particles from this decay process. **[4.85MeV]**

(iii) Why are the answers in (i) and (ii) different?

87. Write down the Boolean Expression for  $Y$  from the figure below.



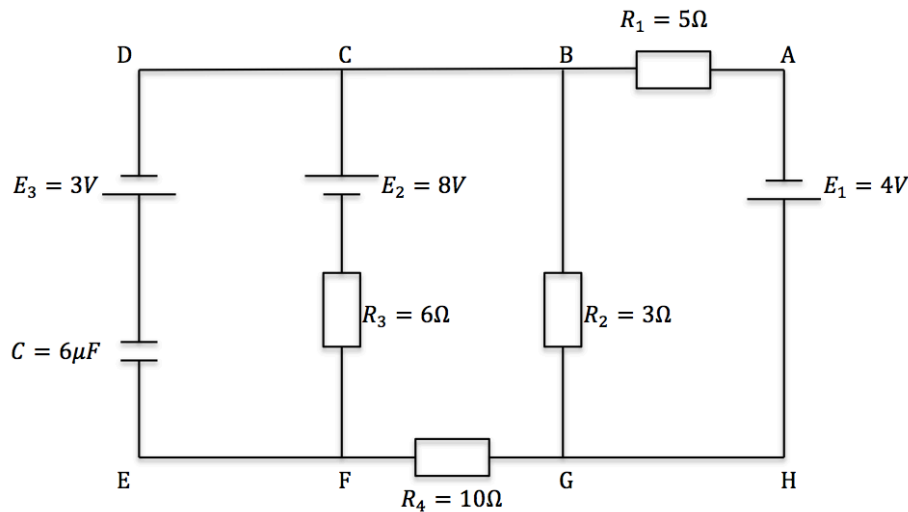
88. Two garages have a common gate that needs to open automatically when a car

is detected to enter either of the garages. Draw a truth table and its equivalent logic gate circuit.

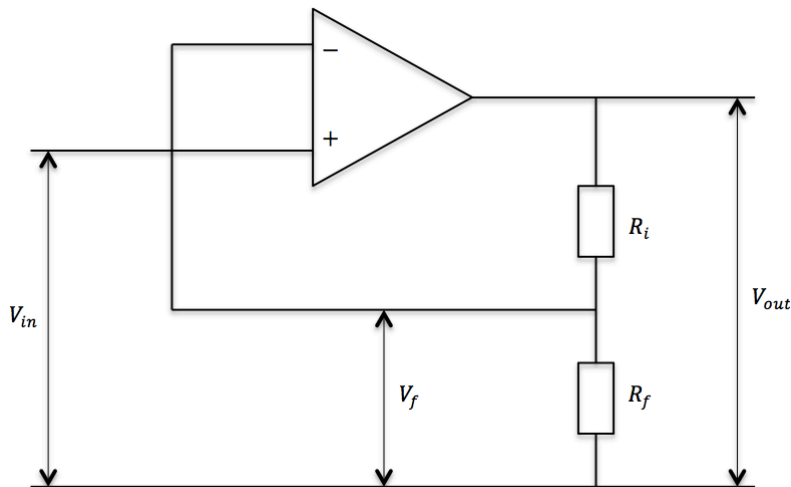
89. Show that de-Broglie wavelength of an electron that has been accelerated through a potential difference  $V$  from rest is approximately given by:

$$\lambda = \frac{12.27}{\sqrt{V}} \text{ \AA}$$

90. The circuit diagram below contains a capacitor, resistors and three cells of negligible internal resistance. Compute the current passing through the  $3\Omega$  resistor and the charge on the capacitor. **[0.168A, 46.86 $\mu$ C]**



91. Explain conduction of electricity in gases  
 92. Study the figure below then answer the questions that follow.



- (i) Show that the gain is given by:  $A = 1 + \frac{R_i}{R_f}$
- (ii) Suppose that  $R_i = 9k\Omega$  and  $R_f = 1k\Omega$ . Calculate the output voltage if the input voltage is  $0.5V$ . [5V]

*'Happy holidays'*